
" HALF-HOUR "
INSTRUCTIONS

For the use of British Made
" UNIQUE "
SLIDE RULES

Containing
CONVERSION TABLE for
MONEY CALCULATIONS

One copy of this Instruction is supplied
Free with each Slide Rule purchased.
Additional copies price Sixpence each.

COPYRIGHT

PRINTED IN ENGLAND

SINCE the operations of multiplication and division occur so frequently in the computation of numerical results, any mechanical means of performing them rapidly is valuable. Various forms of Slide Rules are obtainable, with the aid of which, results, sufficiently accurate for most purposes, may be readily obtained. Compared with ordinary or contracted methods, or the use of logarithms, computation by the Slide Rule is less laborious, less liable to error, and very much more expeditious.

An illustration of the 10in. "Unique" Log-Log Slide Rule is given on pp. 6 and 7 and an inspection of the rule itself shows that the essential parts consist of four scales, denoted for reference in the illustration by the letters A, B, C and D, and a log-log scale running along the top and bottom edges, denoted by LU and LL. A transparent cursor with a fine line drawn across it is supplied to assist in certain operations.

The scales are in all cases divided in decimals, and practice in reading them may be necessary. It is obviously quite impossible to number every division, and in reading a position in any scale the nearest number to the left, or to the right, must be carefully observed, and the divisions of the scale followed until the exact position is reached. For example, in the illustration of the rule, the cursor line is standing at 1.748 in LU, at 31.2 in A, at 37.8 in B, at 6.15 in C, at 5.6 in D, and at 270 in LL.

(The comprehensive numbering of the scales is a distinctive feature of the Unique Slide Rule, and in this respect it is superior to the more expensive instruments, most of which are numbered in an inadequate and misleading manner).

MULTIPLICATION is effected by using scale C in conjunction with scale D. Supposing multiplication of 15 and 45 is desired, the procedure is:—Move the slide so that the 1 on C is brought opposite 15 on D, and read the answer 675 in scale D, opposite 45 in scale C. In some cases when the 1 of scale C is used, the answer is off the scale, and the 10 of scale C must be used instead of the 1. For example, if 25×45 is to be computed, the procedure is:—Set the 10 of C opposite 25 in D and coincident with 45 in C, the result,

1125, will be found in D. Scales A and B may be used for multiplication if desired, the result will always be on the scale, and the slight delay occasioned by the double setting avoided. It is for this reason that the upper pair of scales is sometimes employed in multiplication, but greater accuracy will always be obtained when scales C and D are used, and their use in multiplication and division generally is strongly recommended.

In this example the answer is 1125, but the manipulation of the slide rule would be exactly the same in the multiplication of any two numbers in which two five, and four five are the only significant figures, for example, $25 \times 45 = 1125$; $2.5 \times 45 = 112.5$; $.25 \times 45 = 11.25$; $.025 \times 45 = 1.125$. The position of the decimal point in the answer is easily determined by inspection. When three or more numbers are to be multiplied together, the computation is effected by a series of operations, the cursor line being used to mark the intermediate answers until the final result is reached.

DIVISION. Set the slide so that the divisor on scale C is coincident with the dividend on scale D, the result will be found in D opposite 1 or 10 in C.

For example, suppose it is desired to divide 13.9 by 5.65. Adjust the slide so that 565 in scale C is coincident with 139 in scale D. Opposite 10 in C will be found the result in D, viz., 246. Inserting the decimal point, the result 2.46 is obtained.

In computing the value of an expression such as the following :

$$\frac{86.2 \times .049 \times 18 \times 1.7}{22.5 \times 11.45 \times 8}$$
it is evident that repeated multiplication of the four numbers of the numerator, followed by division separately, by the three numbers of the denominator will give the result, but time is saved by dividing and multiplying alternately. Using scales C and D, find 862 on D, and bring 225 on C into coincidence; adjust cursor line to 18 in C, then move slide to bring 8 on C under cursor line; move cursor line into position above 49 in C and adjust slide so that 1145 in C lies under cursor line; read the answer, 627, in D opposite 17 in C. Approximate

cancellation of the numbers will fix the position of decimal point in the answer. 22.5 divides 86.2 approximately 4, and the 4 thus obtained divides 11.45 nearly 3, which leaves 6 in the numerator when divided into 18; .8 into 1.7 gives roughly 2, and the result is approximately $6 \times 2 \times .05 = 12 \times .05 = .6$. The answer, therefore, is .627.

Frequently the position of decimal point may be determined without resorting to the approximation indicated above, e.g., suppose the fraction $\frac{51.9}{69.7}$ is desired as a percentage. Using the Slide Rule to divide 519 by 697, the result, 745 obtained, is obviously 74.5 per cent.

Those using the Slide Rule for the first time are advised to master the operations of multiplication and division, as explained above, before reading any further. Practice with simple numbers giving results easily checked is recommended, e.g., using scales C and D evaluate $\frac{2 \times 12 \times 6}{4 \times 9}$ and see if the answer is 4. Now repeat, taking the numbers in a different order, and see if the result is the same. Take note of the time saved by dividing and multiplying alternately, as described in the example given earlier. Half-an-hour spent on similar simple examples will suffice to teach the use of the rule for the fundamental operations of multiplication and division.

The following rules, based upon the manipulation of the Slide Rule, are sometimes used to fix the decimal point, but their use is not recommended. In multiplication, when the 1 of scale C is used in the setting of the slide, the number of digits occurring before the decimal point of the answer is one less than the sum of the numbers of digits appearing before the decimal points of the original numbers. When the 10 of scale C is used in setting, the number of digits before the decimal point of the answer is the same as the sum of the numbers of digits preceding the decimal points of the original numbers. When dividing, if the answer appears opposite 1 in C the number of digits preceding the decimal point of the answer is one greater than the difference obtained by

subtracting the number of digits lying before the decimal point of the divisor from the number of digits appearing before the decimal point of the dividend, but if the answer is found opposite 10 in C the number of digits preceding its decimal point is the same as the difference between the numbers of digits appearing before the decimal points of dividend and divisor respectively. When the numbers to be multiplied together or divided are of values less than unity, the number of ciphers immediately following the decimal points must be taken into account and reckoned as negative in the application of the rules for fixing the position of decimal point in the answer.

SQUARES. Numbers may be squared by multiplication direct, but results are more readily obtained by reading in scale A the squares of numbers directly opposite in scale D, the cursor or, preferably the slide, being used to project from one scale to the other.

The calculation of the area of a circle from the diameter is a computation often desired. Find the number representing diameter on D and bring the 1 or 10 of scale C into coincidence with it. The answer appears in A opposite the line at 785 in B.

SQUARE ROOTS. The square roots of all numbers in scale A appear directly below in scale D. Since, however, any number appears twice in scale A, care is necessary in selecting the one to be used. The rule is:—If the original number has an odd number of digits preceding its decimal point, or, when less than unity, has an odd number of ciphers immediately following its decimal point, the left-hand half of scale A must be used. When the number of digits preceding, or the ciphers immediately following the decimal point in the original number is even, the right-hand half of scale A must be used.

CUBES of numbers may be found by repeated multiplication, or more quickly by moving the 1 or 10 of scale C into coincidence with the number to be cubed in D, and reading the answer in A directly opposite the original number in B.

CUBE ROOTS. Find the number whose cube root is required

in scale A and place the cursor line over it. Move the slide until the number in scale B, directly under the cursor line, is exactly the same as that in D opposite 1 or 10 in C. There will be three positions of the slide satisfying these conditions, and care must be taken to select, by inspection, the one giving the correct value.

Squares, square roots, cubes and cube roots may be evaluated with the aid of the log-log scale, sometimes with a higher degree of accuracy than is possible with scales A, B, C and D.

LOGARITHMS.—The common log of any number is obtained by finding the number in the LU or LL scale, placing the cursor line over it and moving the slide so that the number 2.303 in C lies under the cursor line. The log will then be found in D opposite either 1 or 10 of C. Suppose the common log of 18.75 is required :— Place the cursor line over 18.75 in LL, and move the slide until 2.303 in C lies under the cursor line. The log 1.273 appears in D opposite 1 in C. By this method the complete logarithm, characteristic and mantissa is obtained. In certain models there is a gauge mark, denoted by U, at 2.303 in C to assist in finding common logs.

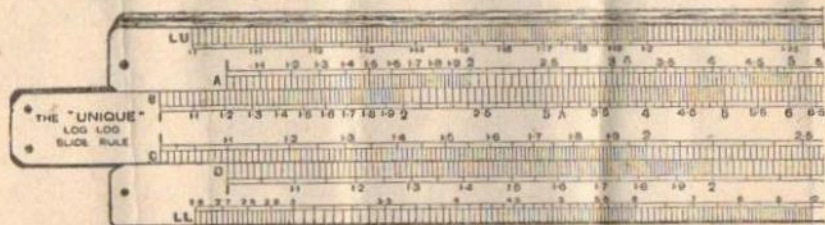
RECIPROCAL SCALE.

Certain types of Log-Log Rules are equipped with a reversed C scale (subsequently referred to as the Cr scale) placed along the middle of the Slide. The uses of this scale are indicated in the following examples :—

Reciprocals are obtained by projecting, from C to Cr or vice versa e.g. 4 in C projects into .25, i.e. $\frac{1}{4}$ in Cr.

Multiplication and Division. To compute the value of an expression such as $2.8 \times 3.2 \times 6.5$, find 2.8 in scale D, then with the aid of the Cursor, bring 3.2 in Cr into coincidence and read the result, 58.2 in D, opposite 6.5 in C, with one setting of the Slide. The factors may be selected in any order and the operations repeated, if necessary, to cover any number of factors.

To find the value of $\frac{82}{3.6 \times .78}$ find 82 in D and bring 36 in C into coincidence. Then opposite 78 in Cr find the result 29.2 in D, the decimal point being inserted by inspection.



LOG-LOG COMPUTATIONS.

The tenth powers of all numbers in LU lie immediately below in LL, and the tenth roots of numbers in LL lie directly above in LU.

Examples (a) $1.8^{10} = 357$

(b) $12^{10} = (1.2 \times 10)^{10} = (1.2^{10})(10^{10}) = 6.2 \times 10^{10}$

(c) ${}^{10}\sqrt{50} = 1.48$

(d) ${}^{10}\sqrt{2} = \frac{{}^{10}\sqrt{20}}{10} = \frac{1.35}{1.259} = 1.072$

NATURAL LOGARITHMS may be obtained by reading opposite the number whose logarithm is desired in LU or LL, the logarithm in D.

Examples (e) $\log e 9 = 2.2$

(f) $\log e 1.5 = .405$

Powers of e may be obtained by reading opposite the exponent in D, the result in LU or LL.

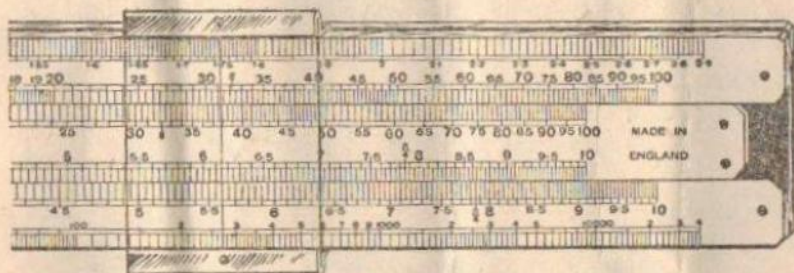
Examples (g) $e^4 = 54.6$

(h) $e^{-3} = 1.35$

(i) $e^{22} = (e^4)^5 = \text{from (g) above } (54.6)^5 = (5.46 \times 10)^5 = 162000$ see (k) below.

Roots of e may be evaluated by using the reciprocal of the exponent in the foregoing rule.

Example (j) ${}^8\sqrt{e} = e^{-.125} = 1.133$



The most useful purpose which the log-log Scale serves is computing powers and roots when exponents are fractional.

Example (k) To evaluate $6.4^{3.21}$

Set the cursor line over 6.4 in LL and bring 1 of C into coincidence with it. Read the answer 387 in LL opposite 3.21 in C, again using the cursor.

Find the value of £86 after $6\frac{1}{2}$ years. Compound Interest at 5% per annum being allowed.

First calculate for £1 capital.

£1 at the end of one year becomes $(1 + .05) = £1.05$, at the end of two years £1 becomes $£1.05 (1 + .05) = £(1.05)^2$, and so on.

At the end of $6\frac{1}{2}$ years, £1 at 5% compound interest becomes $(1.05)^{6\frac{1}{2}}$

Proceeding as at (k) above

$$£(1.05)^{6\frac{1}{2}} = £\left(\frac{2.1}{2}\right)^{6\frac{1}{2}} = \left(\frac{£124}{90.5}\right) = £1.372$$

Now multiply by 86. $86 \times 1.372 = £118$, which is very near the correct amount.

Example (l) To evaluate $\sqrt[5]{30}$

Place the cursor line over 30 in LL, move slide so that 5 in C is brought under the cursor line and read the result 1.973 in LU opposite 10 in C, again using the cursor.

If the answer lies outside the range of the log-log scale, *i.e.*, is greater than 40,000 or less than 1.1, it may be found as indicated below.

Example (m) Evaluate 2.1^{20}

$$\begin{aligned} (2.1)^{20} &= (2.1^4)^5 = (19.45)^5 \text{ see (k)} \\ (19.45)^5 &= (1.945)^5 \times 10^5 = 27.9 \times 10^5 \\ &= 2,790,000 \text{ see (k)} \end{aligned}$$

Alternatively

$$\begin{aligned} (2.1)^{20} &= (2.1^{10})^2 = (1670)^2 \text{ see (a)} \\ (1670)^2 &= (1.670)^2 \times (1000)^2 \\ &= 2.79 \times (1000)^2 \\ &= 2,790,000 \end{aligned}$$

Example (n) Evaluate $1.2^{.13}$

$$1.2^{.13} = \frac{12}{10}^{.13} = \frac{(12)^{.13}}{(10)^{.13}} = \frac{1.38}{1.35} = 1.023$$

If the exponent is negative, proceed as with a positive exponent and then find the reciprocal of the result.

SINES, COSINES, TANGENTS. The table on the back of the LOG-LOG and 5-10 Rules gives values of Sines, Cosines, Tangents and Cotangents, of all angles. Values should be taken from the table and used in computations when necessary.

MONEY CALCULATIONS.

Calculations with sums of money expressed in pounds, shillings and pence are not effected easily by Slide Rule, but if the money values are expressed in the decimal system there are no difficulties.

The conversion tables printed below facilitate such calculations, by providing a simple and rapid method of converting shillings and pence into the decimal equivalents of the pound, and *vice versa*.

The table may be used also for converting cwts. and quarters into decimals of the ton, and *vice versa*.

The smaller table shews pence as decimals of the shilling.

**TABLE FOR CONVERTING SHILLINGS AND PENCE INTO POUNDS
AND HUNDREDWEIGHTS AND QUARTERS INTO TONS.**

PENCE QUARTERS	SHILLINGS or CWTs																			
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	
0																				
1	004	054	104	154	204	254	304	354	404	454	504	554	604	654	704	754	804	854	904	954
2	008	058	108	158	208	258	308	358	408	458	508	558	608	658	708	758	808	858	908	958
3	012	062	112	162	212	262	312	362	412	462	512	562	612	662	712	762	812	862	912	962
4	017	067	117	167	217	267	317	367	417	467	517	567	617	667	717	767	817	867	917	967
5	021	071	121	171	221	271	321	371	421	471	521	571	621	671	721	771	821	871	921	971
6	025	075	125	175	225	275	325	375	425	475	525	575	625	675	725	775	825	875	925	975
7	029	079	129	179	229	279	329	379	429	479	529	579	629	679	729	779	829	879	929	979
8	033	083	133	183	233	283	333	383	433	483	533	583	633	683	733	783	833	883	933	983
9	037	087	137	187	237	287	337	387	437	487	537	587	637	687	737	787	837	887	937	987
10	042	092	142	192	242	292	342	392	442	492	542	592	642	692	742	792	842	892	942	992
11	046	096	146	196	246	296	346	396	446	496	546	596	646	696	746	796	846	896	946	996

PENCE EXPRESSED AS DECIMALS OF A SHILLING.

1d. is .042/-	1d. is .083/-	2d. is .167/-	3d. is .250/-	4d. is .333/-	5d. is .417/-
6d. is .500/-	7d. is .583/-	8d. is .667/-	9d. is .750/-	10d. is .833/-	11d. is .917/-

Copyright

The following examples are designed to illustrate the value of the Slide Rule in this work.

Example 1. Calculate the cost of 43 articles at £3 6s. 10d. each.

In the larger table, in the column headed 6s., and in the line marked 10d., is the number .342. £3 6s. 10d. is therefore £3.342. To multiply 3.342 by 43, set 10 in scale C opposite 3.342 in scale D, then opposite 43 in C will be found 143.7 in D. The result, therefore, is £143.7 or £143 14s., by the slide rule, and the exact amount is £143 13s. 10d.

2. Calculate 28% of £61 10s. To multiply 61.5 by 28, find 61.5 in D and bring 10 of C into coincidence. Opposite 28 in C read 17.22 in D. The result is £17 4s. 5d., which is correct to the nearest penny.

3. Find the cost of 16 tons 3 cwt. 2 quarters of material at £1 2s. 8d. per ton.

The table gives 3 cwt. 2 qrs. as .175 tons and 2s. 8d. as £.133.

Multiply 16.175 by 1.133, using scales C and D, and the result will be found to be £18.33, which converts into £18 6s. 7d., which is within one penny of the exact amount.

4. Find the cost of $15\frac{1}{2}$ yards of material at 8s. $4\frac{1}{2}$ d. per yard.

Using the smaller table, 4d. is seen to be .333s., and $\frac{1}{2}$ d. is .042s., which, added together, give .375s. 8s. $4\frac{1}{2}$ d. is therefore 8.375s. Use scales C and D to multiply 15.5 by 8.375 and the result will be found to be 129.8s., which is £6 9s. 10d. The exact value is £6 9s. $9\frac{1}{2}$ d.

Even when the money amounts must be obtained with absolute correctness the Slide Rule will give a ready means of securing a rapid check on the result, and its value in this connection is obvious.

UNIVERSAL RULES.

In addition to the scales of the Log-Log Rule, universal rules are equipped with **Sine** and **Tangent** scales, denoted by S and T respectively, for trigonometrical calculations.

Sines of angles are found by using the cursor to project from the S scale to the A scale. If the result lies between 1 and 10 of A, the decimal point and a cypher precede the number found in scale A. If the result lies between 10 and 100 in A, the decimal point only should be prefixed.

$$E.g.—\text{Sin } 3^\circ-10' = .0552.$$

$$\text{Sin } 20^\circ-40' = .353.$$

Cosines of angles are obtained by finding the sines of the complementary angles. *E.g.*— $\text{Cos. } 36^\circ = \text{Sin } 54^\circ = .809$.

Tangents of angles are obtained by projecting from the T scale into the D scale, using the cursor. The tangent scale starts just below 6° and finishes at 45° and all values lie between .1 and 1

$$E.g.—\text{Tan } 27^\circ-30' = .521.$$

Tangents of angles between 45° and 90° are obtained easily by finding the reciprocal of the tangent of the complementary angles.

$$E.g.—\text{Tan } 72^\circ = \frac{1}{\text{Tan } 18^\circ} = 3.078.$$

In this case, 18° in the T scale is projected into the Cr scale, with the slide in its central position.

Cosecants, Secants and Cotangents are found as the reciprocals of sines, cosines and tangents respectively.

When sin or tan terms appear as factors, the cursor is used in conjunction with the appropriate angles in the S or T scales.

Example.—The sides of a triangle are 3.5 and 7.2 feet long. The included angle is 25° . The area is required. Place cursor line over 25 in S. Move slide to bring 20 of B under cursor line. Now move cursor to 35 in B. Bring 10 of B under cursor line and read the result : 5.33 sq. feet in A, opposite 7.2 in B.

UNIVERSAL II. RULE.

This rule has the S and T scales on the slide instead of on the stock. For certain calculations this arrangement of scales is more convenient than that of the universal rule, since it allows of multiplication or division of any series of numbers and functions of angles.

NAVIGATIONAL RULE.

This rule has S and T scales on both the slide and the stock. When much trigonometrical work has to be included, such as in navigational calculations, this rule is probably the best obtainable. It is literally unique, and can be obtained only from the manufacturers of these rules.

Detailed instructions are not given here for the Universal II. and the Navigational rules, since the variety of work is extensive, and it is assumed that users of these rules will be familiar with their operation.

5-10 and 10-20 PRECISION RULES.

It is assumed that users of these Rules are familiar with the Slide Rule in its ordinary form.

Slight modifications of the instructions given above are necessary. The log-log instructions do not apply to the precision type of rule, which has no log-log scale.

The C and D scales, which are twice the usual length, are divided into two parts and occupy the positions of the A, B, C and D scales in the standard rule.

Multiplication and Division are effected by the C and D scales, but since numbers on either edge of the slide cannot be brought into direct coincidence with numbers on the opposite side of the

stock, the Cursor must be used in setting the slide in such cases. Otherwise the manipulation of the rule is similar to that of the standard type and any uncertainty in reading the result may be avoided if it is remembered, that **if in setting the rule it is necessary to use the Cursor to cross the slide, it will be necessary to cross the slide again, when reading the result.**

A little practice with simple examples will overcome any initial difficulty.

Squares and Square Roots are obtained easily by projecting from the C and D scales to the scales lying on the edges of the stock.

Logarithms. The mantissa of the logarithm of any number is found by projecting from the C scale to the evenly divided scale lying in the centre of the slide. The figures along the top of this scale are used when the number whose logarithm is required appears in the upper part of the C scale, and the lower figures in the central log scale refer to logs of numbers in the lower C scale. The vernier may be used to read the fourth figure of the mantissa if desired. To use the vernier, move the slide into its central position, *i.e.*, with the ends of the C and D scale coincident. Place the Cursor line over the number whose logarithm is desired, and read the first three figures of the mantissa directly from the log scale. Move the slide to the right, so that the line in the log scale immediately to the left is brought exactly under the Cursor index, and now read the vernier to obtain the fourth figure of the mantissa.

Example (5-10 Rule).—To find the log of 485. Adjust slide to mid-position. Place cursor line over 485, which lies in the lower parts of the C and D scales, and read the log scale, *viz.*, .6840. Move slide so that the line immediately to the left of Cursor is brought under the Cursor index and note that the vernier reading is 17. Add .6840 to .0017 and so obtain the correct mantissa .6857. Now add the characteristic 2 and complete the logarithm, 2.6857.

N.B.—The log scale is omitted from the 10-20 rule, which is designed for great accuracy in ordinary calculations.

The "UNIQUE" range of BRITISH MADE SLIDE RULES

- UNIVERSAL I RULE.** Nine scales: A, B, C and D, Log-Log, Reciprocal, Sin and Tangent. The rule for universal use. 8s. 6d. each.
- UNIVERSAL II RULE.** Scales: A, B, C and D, Log-Log, Sin and Tangent. S and T scales on slide. The rule for Trigonometrical work. 8s. 6d. each.
- 10" LOG-LOG RULE.** Scales: A, B, C and D, Log-Log and Reciprocal (if desired). The popular rule for ordinary purposes. 6s. 0d. each.
- 10" LEGIBLE RULE.** Scales: A, B, C and D only. Specially designed, with wider divisions and slightly heavier lines, for users who find rules with fine divisions trying to the eyes. 6s. 0d. each.
- 5" LOG-LOG RULE.** Scales as in 10" above. The pocket rule for ordinary purposes. 4s. 6d. each.
- 10/20 PRECISION RULE.** A 10" rule equipped with 20" scale and giving 20" accuracy. The rule for the drawing office or when great accuracy is essential. 8s. 6d. each.
- 5/10 PRECISION RULE.** A 5" rule equipped with a 10" scale. The pocket rule for precise calculations. 4s. 6d. each.
- 10" COMMERCIAL RULE (Patent.)** Nine scales. Especially designed for all office calculations. 8s. 6d. each.
- 10" ELECTRICAL RULE.** Specially designed for all engineering calculations. Duplicated C and D scales for high speed operations. 8s. 6d. each.
- NAVIGATIONAL RULE.** Scales: A, B, C and D with Sin and Tangents duplicated. Linear Scales 1:1,000,000, and 1:500,000 in accordance with international practice. The rule for all Navigators. 9s. 6d. each. Special Instructions 2/- extra. Rule including Instructions 11/-.

Postage 3d. extra each rule

Special Rules for advertising purposes
